

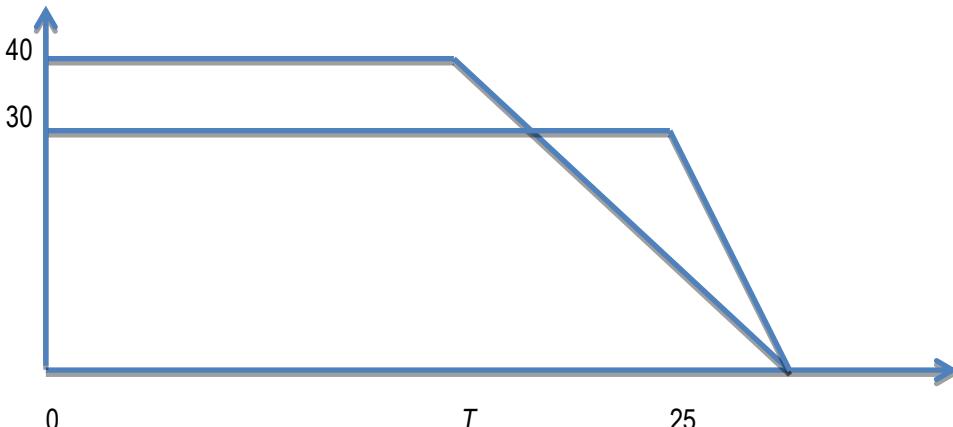
Question Number	Scheme	Marks
1(a)	$\tan \theta = \frac{5}{20}$ $\theta = 14.036..^\circ$ $\theta = 104^\circ \text{ nearest degree}$	M1 A1 A1 (3)
(b)	$\mathbf{p} = 400\mathbf{i} + t(15\mathbf{i} + 20\mathbf{j})$ $\mathbf{q} = 800\mathbf{j} + t(20\mathbf{i} - 5\mathbf{j})$	M1 A1 A1 (3)
(c)	Equate their $\mathbf{j}$ components: $20t(\mathbf{j}) = (800 - 5t)(\mathbf{j})$ $t = 32$ $\mathbf{s} = 800\mathbf{j} + 32(20\mathbf{i} - 5\mathbf{j})$ $= 640\mathbf{i} + 640\mathbf{j}$	M1 A1 M1 A1 (4) <b>10</b>
1(a)	<p style="text-align: center;"><b>Notes</b></p> <p><b>Allow column vectors throughout</b></p> <p>M1 for <math>\tan \theta = \pm \frac{5}{20}</math> or <math>\pm \frac{20}{5}</math> (or any other complete method)</p> <p>First A1 for <math>\pm 14.04^\circ</math> or <math>\pm 75.96^\circ</math></p> <p>Second A1 for <math>104^\circ</math></p>	
1(b) (i) (ii)	M1 for clear attempt at either $\mathbf{p}$ or $\mathbf{q}$ (allow slip but $t$ <u>must</u> be attached to the velocity vector and position vector and velocity vector must be paired up correctly) First A1 $400\mathbf{i} + t(15\mathbf{i} + 20\mathbf{j})$ “ $\mathbf{p} =$ ” not needed but must be clear it's $P$ Second A1 $800\mathbf{j} + t(20\mathbf{i} - 5\mathbf{j})$ “ $\mathbf{q} =$ ” not needed but must be clear it's $Q$	
1(c)	First M1 for equating their $\mathbf{j}$ components; allow $\mathbf{j}$ 's on both sides First A1 for $t = 32$ Second M1 <u>independent</u> for substituting their $t$ value into their $\mathbf{q}$ from (b) Second A1 for $640\mathbf{i} + 640\mathbf{j}$	

Question Number	Scheme	Marks
2(a)	$T - 0.5g - 1.5g = 2 \times 0.5$ $T = 20.6 \text{ (N)} \text{ or } 21 \text{ (N)}$	M1 A1 A1 (3)
(b)	$R - 1.5g = 1.5 \times 0.5$ <p>Force = 15.5 (N) or 15 (N)</p> <p>OR: <math>T - R - 0.5g = 0.5 \times 0.5</math></p> <p>Force = 15.5 (N) or 15 (N)</p>	M1 A1 A1 (3) <b>OR</b> M1 A1 A1 (3) <b>6</b>
<b>Notes</b>		
2(a)	<p><b>N.B.</b> In both parts of this question use the mass which is being used to guide you as to which part of the system is being considered</p> <p>M1 is for an equation for whole system in <math>T</math> only, with usual rules</p> <p>First A1 for a correct equation</p> <p>Second A1 for 20.6 or 21</p>	
2(b)	<p>First M1 is for an equation for the brick only (1<sup>st</sup> alternative) or for the scale pan only (2<sup>nd</sup> alternative) with usual rules.</p> <p>First A1 for a correct equation (in the second alternative <math>T</math> does not need to be substituted)</p> <p>Second A1 for 15.5 or 15</p>	
	<p><b>N.B.</b> If <math>R</math> is replaced by <math>-R</math> in either equation, can score M1A1. This would lead to <math>R = -15.5</math> or <math>-15</math>. The second A1 can then only be scored if the candidate explains why the –ve sign is being ignored.</p>	

Question Number	Scheme	Marks
3.	$F = \frac{1}{8} \times 0.4g$ $-\frac{1}{8} \times 0.4g = 0.4a$ $0 = u^2 + 2(-\frac{1}{8}g) \times 5$ $I = 0.4 \times (3.5 - -4) = 3 \text{ Ns}$	M1 M1 A1 M1 A1 M1 A1 7
	<b>Notes</b>	
3.	First M1 for $1/8 \times 0.4g$ (Allow if $g$ omitted) Second M1 for resolving horizontally with their $F$ (could just be $F$ ) First A1 for a correct equation in $a$ only Third M1 for use of $v^2 = u^2 + 2as$ with $v = 0$ , $s = 5$ and $a$ calculated value of $a$ . (M0 if $u = 4$ or if $u = 0$ ) Second A1 for a correct equation in $u$ only ( $u$ may be in terms of $I$ ) Fourth M1 (M0 if $g$ included or if $u = 0$ or $u = 4$ ) for $\pm 0.4(u - \pm 4)$ where $u$ is their calculated value. Third A1 for 3, 3.0 or 3.00 (Ns)	

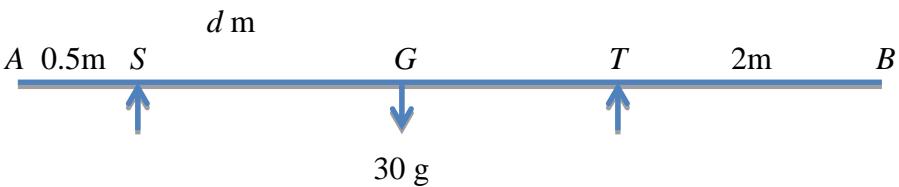
Alternative work –energy method:

$$\begin{aligned}
F &= (\frac{1}{8} \times 0.4g) & \text{M1} \\
: \frac{1}{2} 0.4u^2 &= (\frac{1}{8} \times 0.4g) \times 5 & \text{M2 A2 (M2 if } F \text{ not substituted)} \\
I &= 0.4 \times (3.5 - -4) & \text{M1} \\
&= 3 \text{ (Ns)} & \text{A1}
\end{aligned}$$

Question Number	Scheme	Marks
4(a)		B1 shape (M) B1 figs (40,T) B1 shape (N) B1 figs (30,25) (4)
(b)	<p><b>For N:</b> <math>\frac{1}{2}(25 + 25 + t).30 = 975</math> OR <math>\frac{1}{2}(25 + t_1).30 = 975</math>  <math>t = 15</math> <math>t_1 = 40</math></p> <p><b>For M:</b> <math>\frac{1}{2}(25 + t + T).40 = 975</math> OR <math>\frac{1}{2}(t_1 + T).40 = 975</math>  <math>T = 8.75</math> (<math>8\frac{3}{4}</math> or <math>\frac{35}{4}</math> oe)</p>	M1 A1 DM1 A1 M1 A1 DM1 A1 (8) 12
	ALTERNATIVE: They may find $t$ or $t_1$ , in terms of $T$ , from their (M) equation, and substitute for $t$ or $t_1$ in their (N) equation, and then solve for $T$ :	
	<p><b>For M:</b> <math>\frac{1}{2}(25 + t + T).40 = 975</math> OR <math>\frac{1}{2}(t_1 + T).40 = 975</math>  <math>t = (\frac{1950}{40} - 25 - T)</math> <math>t_1 = (\frac{1950}{40} - T)</math></p> <p><b>For N:</b> <math>\frac{1}{2}(25 + 25 + t).30 = 975</math> OR <math>\frac{1}{2}(25 + t_1).30 = 975</math>  sub for <math>t</math> or sub for <math>t_1</math>  <math>T = 8.75</math> (<math>8\frac{3}{4}</math> or <math>\frac{35}{4}</math> oe)</p>	M1 A1 DM1 A1 M1 A1 DM1 A1 (8) 12
4(a)	Notes First B1 (M) for correct shape – <i>must start and finish on the axes</i> . Second B1 for 40 and $T$ marked clearly (if delineators omitted B0) and correctly Third B1 (N) for correct shape – <i>must start and finish on the axes</i> . Fourth B1 for 30 and 25 (if delineators omitted B0) marked clearly and correctly <b>N.B.</b> If graphs do not cross and/or do not finish at the same point, max score is B1B1B0B1.	

	<p><b>N.B.</b> If graphs done on separate diagrams, mark each and award the higher mark i.e. can score max 2/4 for part (a).</p>	
4(b)	<p><b>N.B.</b> When attempting to find the area of a triangle, must see <math>\frac{1}{2} x</math> .... to be able to award an M mark i.e. M0 if <math>\frac{1}{2}</math> is missing</p> <p><b>N.B.</b> When attempting to find the area of a trapezium, must see something of the form : <math>\frac{1}{2} x (a + b)h</math> to be able to award an M mark i.e. M0 if <math>\frac{1}{2}</math> is missing and bracket is not a <b>sum</b></p> <p>First M1 for attempt at using 975m distance travelled by <math>N</math> to obtain an equation in one unknown <i>time</i> (usually extra time <math>t</math> after 25 s, but could, for example, be whole time <math>t_1</math>). They may use the area under their graph or use <i>suvat</i> (<b>N.B.</b> Any single <i>suvat</i> equn using <math>s = 975</math> is M0).</p> <p>First A1 for a correct equation in their unknown <i>time</i>  e.g. <math>(30 \times 25) + \frac{1}{2} 30t = 975</math> <b>OR</b> <math>(30 \times 25) + \frac{1}{2} 30(t_1 - 25) = 975</math></p> <p>Second M1, dependent on first M, for solving their equation</p> <p>Second A1 for a correct value for their unknown.</p> <p>Third M1 for attempt at using 975m distance travelled by <math>M</math> to obtain an equation in <math>T</math> and possibly one other unknown <i>time</i> (usually extra time <math>t</math> after 25 s, but could, for example, be whole time <math>t_1</math>). They may use the area under their graph or use <i>suvat</i> (<b>N.B.</b> Any <i>suvat</i> equn using <math>s = 975</math> is M0)</p> <p>Third A1 for a correct equation in <math>T</math> and possibly their unknown. This A1 can be earned if they just have a letter for their unknown :-  e.g. <math>40T + \frac{1}{2} 40.(25 + t - T) = 975</math> <b>OR</b> <math>40T + \frac{1}{2} 40.(t_1 - T) = 975</math> or <u>for an incorrect numerical value in place of <math>t</math> or <math>t_1</math></u>.</p> <p>Fourth M1, dependent on first, second and third M's, for solving for <math>T</math>.</p> <p>Fourth A1 for 8.75 or <math>35/4</math> or any other equivalent</p> <p>SEE MARKS FOR ALTERNATIVE ABOVE.</p>	

Question Number	Scheme	Marks
5.	$mR$ $R = 2g \cos 20^\circ + 40 \cos 60^\circ$ $F = 40 \cos 30^\circ - 2g \cos 70^\circ$ $m = \frac{40 \cos 30^\circ - 2g \cos 70^\circ}{2g \cos 20^\circ + 40 \cos 60^\circ}$ $= 0.73 \text{ or } 0.727$	B1 M1 A2 M1 A2 M1 M1 A1 <b>10</b>
<b>Notes</b>		
5.	B1 for $\mu R$ seen or implied.	
	First M1 for resolving perpendicular to the plane with usual rules (must be using 2(g) with $20^\circ$ or $70^\circ$ and 40 with $30^\circ$ or $60^\circ$ )	
	First and second A1's for a correct equation. A1A0 if one error	
	Second M1 for resolving parallel to the plane with usual rules (must be using 2(g) with $20^\circ$ or $70^\circ$ and 40 with $30^\circ$ or $60^\circ$ )	
	Third and fourth A1's for a correct equation. A1A0 if one error	
	Third M1 <u>independent</u> for eliminating $R$ to produce an equation in $\mu$ only. Does not need to be $\mu = \dots$	
	Fourth M1 <u>independent</u> for solving for $\mu$	
	Fifth A1 for 0.727 or 0.73	
	<b>N.B.</b> They may choose to resolve in 2 other directions e.g. horizontally and vertically.	
	<b>N.B.</b> If $F$ is replaced by $-F$ in the second equ <sup>n</sup> , treat this as an error unless they subsequently explain that they have their $F$ acting in the wrong direction, in which case they could score full marks for the question.	

Question Number	Scheme	Marks
6.	 $M(S): Mg \cdot 0.5 = 30g(d - 0.5)$ $M(T): Mg \cdot 2 = 30g(4 - d)$ <div style="display: flex; align-items: center; justify-content: space-between;"> <span>dividing:</span> <math display="block">4 = \frac{(4 - d)}{(d - 0.5)} \Rightarrow \begin{aligned} \text{(i)} \quad d &amp;= 1.2 \\ \Rightarrow \text{(ii)} \quad M &amp;= 42 \end{aligned}</math> </div>	M1 A1 M1 A1 <b>DM1 A1</b> A1
6.	<p><b>Notes</b></p> <p><b>N.B.</b> They may use a different variable, other than <math>d</math>, in their moments equations  e.g. say they use <math>x = SG</math> consistently, they can score all the marks for their two equations and if they eliminate <math>x</math> correctly, DM1 A1 (for <math>M</math>), and, if they found <math>x</math> correctly, then added 0.5 to obtain <math>d</math>, the other A1 also.</p>	
	First M1 for moments about $S$ (need correct no. of terms, so if they don't realise that the reaction at $T$ is zero it's M0) <i>to give an equation in <math>d</math> and <math>M</math> only.</i>	
	First A1 for a correct first equation <i>in <math>d</math> and <math>M</math> only</i> . (A1 for both g's or no g's but A0 if one g is missing)	
	<p><b>N.B.</b> They may use 2 equations and eliminate to obtain their equation <i>in <math>d</math> and <math>M</math> only</i>  e.g. <math>M(A) 0.5R_S = 30gd</math> and <math>(^) R_S = 30g + Mg</math> and then eliminate <math>R_S</math>.  The M mark is only earned once they have produced an equation <i>in <math>d</math> and <math>M</math> only</i>, with all the usual rules about correct no. of terms etc applying to all the equations they use to obtain it.</p>	
	Second M1 for moments about $T$ (need correct no. of terms, so if they don't realise that the reaction at $S$ is zero it's M0) <i>to give an equation in <math>d</math> and <math>M</math> only</i>	
	Second A1 for a correct second equation <i>in <math>d</math> and <math>M</math> only</i> . (A1 for both g's or no g's but A0 if one g is missing)	
	<p><b>N.B.</b> They may use 2 equations and eliminate to obtain their equation <i>in <math>d</math> and <math>M</math> only</i>  e.g. <math>M(B) 2R_T = 30g(6 - d)</math> and <math>(^) R_T = 30g + Mg</math> and then eliminate <math>R_T</math>.  The M mark is only earned once they have produced an equation <i>in <math>d</math> and <math>M</math> only</i>, with all the usual rules about correct no. of terms etc applying to all the equations they use to obtain it.</p>	

	Third M1, <u>dependent on 1<sup>st</sup> and 2<sup>nd</sup> M marks</u> , for eliminating either $M$ or $d$ to produce an equation in either $d$ only or $M$ only.	
	Third A1 for $(d =) 1.2$ oe ( <b>N.B.</b> Neither this A mark nor the next one can be awarded <u>if there are any errors in the equations.</u> ) <b>Beware:</b> If one $g$ is missing consistently from each of their equations, they can obtain $d = 1.2$ but award A0	
	Fourth A1 for $(M =) 42$	
	Scenario 1: Below are the possible equations, (if they don't use $M(S)$ ), any two of which can be used, by eliminating $R_S$ , to obtain an equation <i>in d and M only</i> , for the first M1. N.B. If $R_T$ appears in any of these and doesn't subsequently become zero then it's M0.	
	$M(A) \quad 0.5R_S = 30gd$	
	$M(B) \quad 5.5R_S = 30g(6 - d) + 6Mg$	
	$M(T) \quad 3.5R_S = 30g(4 - d) + 4Mg$	
	$(^) \quad R_S = 30g + Mg$	
	Scenario 2: Below are the possible equations, (if they don't use $M(T)$ ), any two of which can be used, by eliminating $R_T$ , to obtain an equation <i>in d and M only</i> , for the second M1. N.B. If $R_S$ appears in any of these and doesn't subsequently become zero then it's M0.	
	$M(A) \quad 4R_T = 30gd + 6Mg$	
	$M(B) \quad 2R_T = 30g(6 - d)$	
	$M(S) \quad 3.5R_T = 30g(d - 0.5) + 5.5Mg$	
	$(^) \quad R_T = 30g + Mg$	

Question Number	Scheme	Marks
7(a)	$\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ $(-1+a)\mathbf{i} + (2+b)\mathbf{j}$ $\frac{-1+a}{2+b} = \frac{1}{3}$ $a = b = k = 2.5; \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$ <b>ALTERNATIVE:</b> $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ $(-1+a)\mathbf{i} + (2+b)\mathbf{j} = p(\mathbf{i} + 3\mathbf{j})$ $-1+a = p$ $2+b = 3p$ $a = b = k = 2.5; \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$	B1 M1 DM1 A1 DM1 A1; A1 (7)
(b)	$\mathbf{v} = 3\mathbf{i} - 22\mathbf{j} + 3(3\mathbf{i} + 9\mathbf{j})$ $= 12\mathbf{i} + 5\mathbf{j}$ $ \mathbf{v}  = \sqrt{12^2 + 5^2} = 13 \text{ ms}^{-1}$	M1 A1 M1 A1 <b>cso</b> (4)  <b>11</b>
	<b>Notes</b>	
7(a)	<p>B1 for <math>\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}</math> (<math>k \neq 1</math>) seen or implied in working, including for an incorrect final answer, with the wrong <math>k</math> value.</p> <p>First M1 for adding the 2 forces (for this M mark we only need <math>\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}</math>), with <math>\mathbf{i}</math>'s and <math>\mathbf{j}</math>'s collected (which can be implied by later working) but allow a slip.</p> <p><u>(M0 if <math>a</math> and <math>b</math> both assumed to be 1)</u></p> <p>Second M1, dependent on first M1, for ratio of their cpts = 1/3 or 3/1 (Must be correct way up for the M mark)</p> <p>First A1 for a correct equation which may involve two unknowns</p> <p>Third M1, dependent on first and second M1, for solving for <math>k</math> oe</p> <p>Second A1 for a correct <math>k</math> value</p> <p>Third A1 for <math>2.5\mathbf{i} + 2.5\mathbf{j}</math></p>	

**ALTERNATIVE: Using two simultaneous equations**

B1 for  $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$  ( $k \neq 1$ ) seen or implied in working.

First M1 for adding the 2 forces (for this M mark we only need  $\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}$ ), with  $\mathbf{i}$ 's and  $\mathbf{j}$ 's collected (LHS of equation) (M0 if a and b both assumed to be 1) but allow a slip

Second M1, dependent on first M1, for equating coeffs to produce *two* equations in 2 or 3 unknowns. Must have  $p$  and  $3p$  (M0 if p is assumed to be 1 or k)

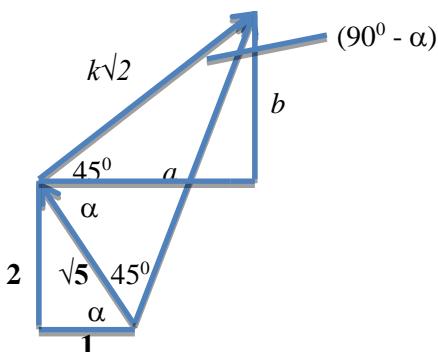
First A1 for two correct equations

Third M1, dependent on first and second M1, for solving for  $k$  oe

Second A1 for a correct  $k$  value

Third A1 for  $2.5\mathbf{i} + 2.5\mathbf{j}$

**ALTERNATIVE: Using magnitudes and directions**



$\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ , seen or implied

Correct vector triangle

$$\frac{k\sqrt{2}}{\sin 45^\circ} = \frac{\sqrt{5}}{\sin(90^\circ - \alpha)}, \quad \alpha = \arctan 2$$

$$2k = 5$$

$$k = 2.5; \quad \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$$

B1

M1

**DM1 A1**

**DM1 A1; A1 (7)**

**ALTERNATIVE: Using magnitudes and directions**

B1 for  $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$  seen or implied in working.

First M1 for a correct vector triangle (for this M mark we only need  $\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}$ ). (M0 if a and b both assumed to be 1 and/or longest side is assumed to be  $\sqrt{10}$ )

Second M1, dependent on first M1, for using sine rule on vector triangle

First A1 for a correct equation.  $45^\circ$  may not appear exactly.

Third M1, dependent on first and second M1, for solving for  $k$  oe

Second A1 for a correct  $k$  value

Third A1 for  $2.5\mathbf{i} + 2.5\mathbf{j}$

(b)	First M1 for use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ with $t = 3$ First A1 for $12\mathbf{i} + 5\mathbf{j}$ seen or implied. However, if a wrong $\mathbf{v}$ is seen A0 Second M1 for finding magnitude of their $\mathbf{v}$ Second A1 for 13	

Question Number	Scheme	Marks
8(a)	$F = \frac{1}{5}R$ $R = 1.5g$ $T - F = 1.5a$ $3g - T = 3a$ $T = 1.2g \text{ or } 11.8 \text{ N or } 12 \text{ N}$	M1 B1 M1 A1 M1 A1 <b>DM1 A1</b> (8)
(b)	$R = \sqrt{T^2 + T^2} \text{ or } 2T \cos 45^\circ \text{ or } \frac{T}{\cos 45^\circ}$ $= 16.6 \text{ (N) or } 17 \text{ (N) or } \frac{6g\sqrt{2}}{5}$ <p style="text-align: center;">Direction is <math>45^\circ</math> below the horizontal oe</p>	M1 A1 A1 B1 (4) <b>12</b>
<b>Notes</b>		
8(a)	First M1 for <i>use of</i> $F = \frac{1}{5}R$ in an equation. B1 for $R = 1.5g$ Second M1 for resolving horizontally with usual rules First A1 for a correct equation Third M1 for resolving vertically with usual rules Second A1 for a correct equation <b>N.B.</b> Either of the above could be replaced by a <i>whole system</i> equation: $3g - F = 4.5a$ <b>N.B.</b> All of the marks for the two equations can be scored if they consistently use $-a$ instead of $a$ . Fourth M1 dependent on first, second and third M marks for solving their equations for $T$ Third A1 for 1.2g, 11.8 (N) or 12 (N)	
(b)	First M1 for a complete method for finding the magnitude of the resultant ( <b>N.B.</b> M0 if different tensions used), First A1 for $\sqrt{T^2 + T^2}$ or $2T \cos 45^\circ$ Second A1 for 16.6(N) or 17 (N) B1 for $45^\circ$ below the horizontal or a diagram with an arrow and a correct angle. Ignore subsequent wrong answers e.g. a bearing of $225^\circ$ , which scores B0, as does SW etc.	